

# Worksheet 1, Math 1A

## Limits

Monday, September 16, 2013

1. Evaluate the limit if it exists:

(a)  $\lim_{t \rightarrow 1} \frac{t^4 - 1}{t^3 - 1}$

(b)  $\lim_{t \rightarrow 0} \left( \frac{1}{t} - \frac{1}{t^2 + t} \right)$

(c)  $\lim_{h \rightarrow 0} \frac{(2 + h)^3 - 8}{h}$

(d)  $\lim_{x \rightarrow -4} \frac{\sqrt{x^2 + 9} - 5}{x + 4}$

2. Prove that  $\lim_{x \rightarrow 0^+} \sqrt{x} e^{\sin(\pi/x)} = 0$ .

3. Prove that  $\lim_{x \rightarrow 2} (x^2 - 4x + 5) = 1$  using the  $\epsilon, \delta$  definition of a limit.

4. Use the definition of continuity and the properties of limits to show that the function  $f(x) = 2\sqrt{3-x}$  is continuous on the interval  $(-\infty, 3]$ .

5. Find a continuous function  $g : \mathbb{R} \rightarrow \mathbb{R}$  which is equal to  $f(x) = (x^2 - x - 2)/(x - 2)$  wherever  $f$  is defined.

6. Prove that cosine is a continuous function.